

# **Mathematics**

Paper 3 (Calculator)

**Higher Tier** 

Tuesday 13 June 2017 - Morning

Time: 1 hour 30 minutes

Paper Reference

1MA1/3H

**You must have:** Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Total Marks 39 39

#### **Instructions**

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You must show all your working.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- Calculators may be used.
- If your calculator does not have a  $\pi$  button, take the value of  $\pi$  to be 3.142 unless the question instructs otherwise.

#### Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
   use this as a guide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶



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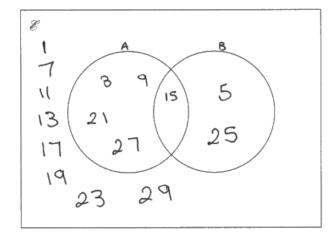


#### Answer ALL questions.

### Write your answers in the spaces provided.

## You must write down all the stages in your working.

- 1  $\mathscr{E}$ = {odd numbers less than 30}
  - $A = \{3, 9, 15, 21, 27\}$
  - $B = \{5, 15, 25\}$
  - (a) Complete the Venn diagram to represent this information.



44 🗸 4

A number is chosen at random from the universal set, &.

(b) What is the probability that the number is in the set  $A \cup B$ ?



15

2) 2 |

Q01b

2

Q01a

(Total for Question 1 is 6 marks) 6

,



$$3x + y = -4$$
$$3x - 4y = 6$$

$$-3x + y = -4$$

$$-3x - 4y = 6$$

$$-5y = 10$$

$$\times -1 \times -1$$

$$5y = -10$$

$$3x = -2 = -4$$
  
 $+2 + 2$   
 $3x = -2$   
 $3x = -1.5$ 

$$v = -2$$

(Total for Question 2 is 3 marks 2 2

3 The table shows some information about the dress sizes of 25 women.

Dress size	Number of women
8	2
10	9
12	8
14	6

(a) Find the median dress size.

2		
(1) 1	~	1

Q03a

3 of the 25 women have a shoe size of 7

Zoe says that if you choose at random one of the 25 women, the probability that she has either a shoe size of 7 or a dress size of 14 is  $\frac{9}{25}$  because

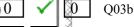
$$\frac{3}{25} + \frac{6}{25} = \frac{9}{25}$$

(b) Is Zoe correct?

You must give a reason for your answer.

Zoe	is correct,	this is	s because	رها ا	are increasing
()	1-1-1-1	lati	adding	J	
the	probability	69	accing.		

(Total for Question 3 is 2 marks) 1



He bakes only vanilla cakes, banana cakes, lemon cakes and chocolate cakes.

 $\frac{2}{7}$  of the cakes are vanilla cakes.

35% of the cakes are banana cakes.

The ratio of the number of lemon cakes to the number of chocolate cakes is 4:5

Work out the number of lemon cakes Daniel bakes.

$$\frac{420}{7} \times 2 = 120$$

$$\frac{420}{100} \times 35 = 147 \qquad \frac{420}{147}$$

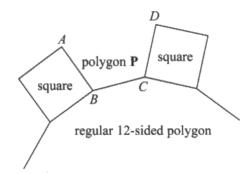
Vanilla=120

68 lemon

(Total for Question 4 is 5 marl

0

5 In the diagram, AB, BC and CD are three sides of a regular polygon P.



Show that polygon **P** is a hexagon. You must show your working.

(Total for Question 5 is 4 marks)



The density of apple juice is 1.05 grams per cm<sup>3</sup>.

The density of fruit syrup is 1.4 grams per cm<sup>3</sup>.

The density of carbonated water is 0.99 grams per cm<sup>3</sup>.

25 cm<sup>3</sup> of apple juice are mixed with 15 cm<sup>3</sup> of fruit syrup and 280 cm3 of carbonated water to make a drink with a volume of 320 cm3.

Work out the density of the drink. Give your answer correct to 2 decimal places.

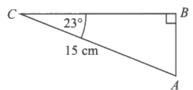
 1.0	<b>1</b>	g/cm <sup>3</sup>

(Total for Question 6 is 4 marks)

7 ABC is a right-angled triangle.

SP	CA	TA		
57	H	14	2	~

Q07



Calculate the length of AB.

Give your answer correct to 3 significant figures.

$$Sin(23) = \frac{3c}{15}$$
  
 $Sin(23) \times 15 = 3c$   
= 5.860966927  
= 46.5.86 35F

5.86 cm

(Total for Question 7 is 2 marks) 2

A square, with sides of length x cm, is inside a circle. Each vertex of the square is on the circumference of the circle.

1 🗸 []

Q08

The area of the circle is 49 cm<sup>2</sup>.

Work out the value of x.

Give your answer correct to 3 significant figures.

$$T_{x}r^{2} = 49$$

$$r^{2} = \frac{49}{37}$$

$$r = \sqrt{\frac{49}{327085}}$$

$$= 3.949327085$$

Area 29

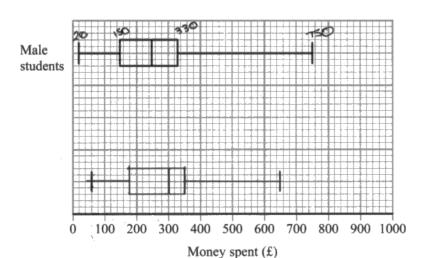
(Total for Question 8 is 4 marks)

9 The box plot shows information about the distribution of the amounts of money spent by some male students on their holidays.



Q09a

Q09b Q09c



(a) Work out the interquartile range for the amounts of money spent by these male students.





The table below shows information about the distribution of the amounts of money spent by some female students on their holidays.

	Smallest	Lower quartile	Median	Upper quartile	Largest
Money spent (£)	60	180	300	350	650

(b) On the grid above, draw a box plot for the information in the table.

(2)

L	
nris	says.

"The box plots show that the female students spent more money than the male students."

## (c) Is Chris correct?

Give a reason for your answer.

because I Chris is This is because the interquartile range for students is greater than female students

male students range is Furthermore, the range: student's the female

(Total for Question 9 is 5 marks)4

10 Naoby invests £6000 for 5 years.

The investment gets compound interest of x% per annum.

At the end of 5 years the investment is worth £8029.35

Work out the value of x.

$$6000 \times \infty^5 = 8029.35$$

$$x^5 = 1.338225$$

= 1.8599999905

$$x = 1.0599999995$$
  
 $x = 1.062dp$ 

1.06

(Total for Question 10 is 3 marks

Q10

11 Jeff is choosing a shrub and a rose tree for his garden.

At the garden centre there are 17 different types of shrubs and some rose trees.

0

Q11

Jeff says,

"There are 215 different ways to choose one shrub and one rose tree."

Could Jeff be correct?

You must show how you get your answer.

No, because

(Total for Question 11 is 2 marks) 0

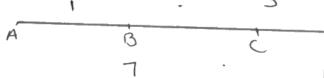
Q12

12 The points A, B, C and D lie in order on a straight line.

a straight line. Total
$$AB:BD = 1:5$$
 6

Work out AB:BC:CD

5



11

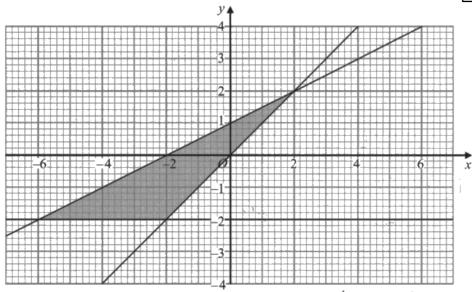
24

1:20:9.3:14.6

(Total for Question 12 is 3 marks)

0

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Write down the three inequalities that define the shaded region.  $y = \frac{1}{2}x + 1$  y = mx + c

$$y = \infty$$
  
 $y = 1 \infty + C$   
 $4 = 4 + 0$ 

 $\frac{9}{9} = 2$   $\frac{9}{2} = 2$   $\frac{9}{2} = 2$ (Total for Question 13 is 4 marks) 3

**14** (a) Simplify 
$$\frac{x^2 - 16}{2x^2 - 5x - 12}$$

$$ax^2 + bx + c$$

## (b) Make v the subject of the formula $w = \frac{15(t-2v)}{v}$

$$w = \frac{18(c - 20)}{\sqrt{2}}$$

$$WV = 15(t-2V)$$

$$\div 15 \qquad \div 15$$

$$\frac{WV}{15} = + -20$$

$$w = \frac{15(t-2v)}{v}$$

$$xv = \frac{15(t-2v)}{xv}$$

$$wv = 15(t-2v)$$

$$vv = 15(t-2v)$$

$$vv = 15(t-2v)$$

$$vv = 15t - wv$$

$$WV + 300 = 15+$$

(3)

(Total for Question 14 is 6 marks)

The area of triangle ABC is  $6\sqrt{2}$  m<sup>2</sup>.

Calculate the value of x.

Give your answer correct to 3 significant figures.

$$+ 4x^{2} - 4x + 1$$
  
+  $x^{2} + 6x + 9$ 

$$-5x^2 + 2x + 10$$
  
 $-4x^2 + 10x - 6$ 

$$(2\alpha - 1)(2\alpha - 1)$$

$$(x+3)(x+3)$$

$$(2x+6)(2x-1)$$

$$(2x+6)(2x-1)$$
  
 $4x^2-2x+12x-6$   
 $4x^2+10x-6$ 

(Total for Question 15 is 5 marks)

0 🗸

Q15

16 Using 
$$x_{n+1} = -2 - \frac{4}{x_n^2}$$
  
with  $x_0 = -2.5$ 

(a) find the values of  $x_1$ ,  $x_2$  and  $x_3$ 

$$\alpha_{3}^{*} = (-2) - \frac{4}{(-2.64)^{3}}$$

$$= -\frac{2803}{1089}$$

$$= -2.5739210284664830119375$$

$$\alpha_3 = (-2) - \frac{4}{(AW5)^2}$$
  
= -2.603767255  
= -2.60 2dp

$$x_{1} = -2.64$$

$$x_{2} = -2.60$$

$$x_{3} = -2.60$$

(b) Explain the relationship between the values of  $x_1$ ,  $x_2$  and  $x_3$  and the equation  $x^3 + 2x^2 + 4 = 0$ 

As you input values into  $x_{n+1} = -2 - \frac{4}{x^2}$  you graduly get closer to the solutions of  $x^3 + 2x^2 + 4 = 0$ .

(Total for Question 16 is 5 marks) 4

1 Q16b

Q16a

17 A train travelled along a track in 110 minutes, correct to the nearest 5 minutes.

Jake finds out that the track is 270 km long.

He assumes that the track has been measured correct to the nearest 10 km.

(a) Could the average speed of the train have been greater than 160 km/h? You must show how you get your answer.

$$\frac{55}{23} \times 60 = \frac{3800}{23} = 143.4782609$$

143.48 mylis the upper bound of the average speed and it is lower than 160 m/h



Jake's assumption was wrong.

The track was measured correct to the nearest 5 km.

(b) Explain how this could affect your decision in part (a).

could increase the answer to part a as you

increasing the number. Therefore it could increase

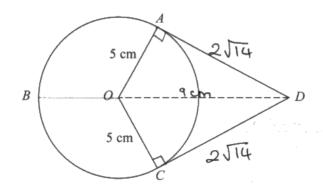
average speed, making me

Q17b

mind

(Total for Question 17 is 5 marks)

18



A, B and C are points on a circle of radius 5 cm, centre O.

DA and DC are tangents to the circle.

$$DO = 9 \text{ cm}$$

Work out the length of arc ABC.

Give your answer correct to 3 significant figures.

$$q^2 - 5^2 = 56$$
 $\sqrt{56} = 2\sqrt{14}$ 

cm

Q18

(Total for Question 18 is 5 marks) 1

**19** Solve  $2x^2 + 3x - 2 > 0$ 

- b = 16-4ac Qa

 $2x^2 + 3x - 2 > 0$ 

 $ax^2 + bx + C$ 

(x) (x)

 $-3\pm\sqrt{3^2-4\times2\times(-2)}$ 

2×2

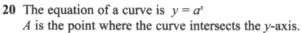
+ = 1/2

-1/2 ,2

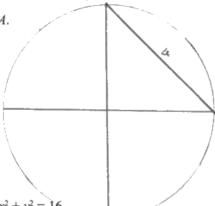
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2>0>-1/2

(Total for Question 19 is 3 marks) 1



(a) State the coordinates of A.



(32, 0)

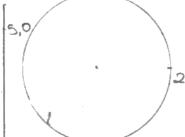
The equation of circle C is  $x^2 + y^2 = 16$ 

The circle **C** is translated by the vector  $\begin{pmatrix} 3 \\ 0 \end{pmatrix}$  to give circle **B**.

(b) Draw a sketch of circle B.

Label with coordinates

the centre of circle  $\bf B$  and any points of intersection with the x-axis.



3) 0

0 Q20b

Q20a

(Total for Question 20 is 4 marks) 0

TOTAL FOR PAPER IS 80 MARKS

20

